# Towards a Taxonomy of MOF Structures

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M. O'Keeffe & O. M. Yaghi, Chem. Rev. 112, 675 (2012) M. Li, D. Li, M. O'K. & O. M. Y., Chem. Rev. 114, 1343 2014) Nothing exists except atoms and empty space,

all else is opinion.

Democritus

### The cluster in basic zinc acetate (a salt!)



In the acetate each carboxylate C atom (black) is joined to a methyl group -> discrete molecule The C atoms are *points of extension* 

H. Koyama, Y. Saito, *Bull.Chem. Soc. Japan* 27, 112 (1954)

In MOF-5 the basic zinc acetate clusters are joined by ditopic linkers (terephthalate) to make an infinite crystal.



H. Li, M. Eddaoudi, M. O'Keeffe, O. M. Yaghi, Nature, 1999, 402, 276

MOF has at least two components. Secondary building units (SBUs)

1. metal-containing ("cation")

0-periodic: single atom or cluster (may be a ring)1-periodic: rod2-periodic: layer3-periodic: usually the whole crystal

2. organic linker (anion")

ditopic polytopic polytopic branched



Cationic clusters and SBUs (red)

[SBU = Secondary Building Unit. Blue polyhedra are metal-O]

metal atoms in an SBU have points of extension in common



Organic polytopic linkers (top) and SBUs (bottom)

[SBU = Secondary Building Unit]



WARNING! An extraordinary Zn<sub>8</sub> SBU reported Sen, S.; Nair, N. M.; Yamada, T.; Kitagawa, H.; Bharadwaj, K. JACS **2012**, *124*, 19432-19437.



Ball and stick model  $Zn_8O(-CO_2)_6 Zn...Zn$  (blue) = 2.0 Å!



Look at thermal ellipsoids – give away for positional disorder!



### The two simplest types of MOF topology



## The simplest type of MOF topology





two structures with the same underlying topology (net)





An iron terephthalate MOF-235 O. M. Yaghi group Inorg. Chem. 44, 2998 (2005) The underlying net scs shown as acs-a The only way of linking trigonal prisms with one kind of link We know "all" the ways of linking shapes by one kind of linker. For example 9 ways of so linking squares.

Can we control which structure we get?

M. Eddaoudi, J. Kim, M. O'Keeffe, O. M. Yaghi et al. Proc. Natl. Acad. Sci. 99, 4000 (2002).

H. Furukawa, J. Kim, N, W. Ockwig, M. O'Keeffe, O. M. Yaghi, *J. Am. Chem. Soc.* 130, 1650 (2008).

Control of periodicity linking paddle wheels (squares) with dicarboxylic acids



#### cuboctahedron



### MOP-1 Framework = $[Cu_2(C_6H_4(COO)_2)_2]_{12}$

M. Eddaoudi, J. Kim, J. B. Wacher, H. K. Chae, M. O'Keeffe, O. M. Yaghi. JACS, 123, 4368-9 (2001).

#### truncated octahedron needs 90°



Z. Ni, O. M. Yaghi.et al. JACS 127, 12752 (2005)

#### A 1-periodic (rod) structure



O. M. Yaghi group J. Am. Chem. Soc. 2008, 130, 11650

#### A 2-periodic (planar) structure



MOF-2 ZnBDC (BDC = benzenedicarboxylate Li. H.; Eddaoudi, M.; Groy, T. L.; Yaghi, O. M. *JACS*, **1998**, *120*, 8571 *How to make a 3-periodic structure* 



Paddlewheels (square SBUs) linked with a twist to produce....



#### MOF-88 Cu(OOC-C<sub>6</sub>H<sub>3</sub>Br-COOO)·H<sub>2</sub>O

Linked paddle-wheel clusters producing a decorated **nbo** net

M. Eddaoudi, J. Kim, M. O' Keeffe, O. M. Yaghi, J. Am. Chem. Soc. 124, 576 (2002)

Transitivity vertex- (edge-) transitive means one topological kind of vertex (edge)

The most important nets with one or two kinds of vertex are edge-transitive

More complex nets are often

minimal transitivity

(see later)

## A second simple type of MOF topology: two vertices one link



Net is tbo-a

linking square and triangle



tbo-a

HKUST-1 linked paddlewheel and benzene tribenzoate  $(Cu_2)_3(btb)_4$ 



S. S.-Y. Chui, S. M. – F. Lo; J. P. H. Charmant, A. G. Orpen, I. D. Williams, Science 283, 1148 (1999)



# An isoreticular series based on tbo



### H. Furukawa etal. Inorg. Chem. 2011, 50, 9147



HKUST-1 very nicely has just the right space for Keggin ions  $AB_{12}O_{40} - A = P$ , As, Si, Ge (tetrahed.) B – Mo, W (octahed.) Zhou-Min Su et al. JACS, 2009, 131. 1884

linking square and triangle



pto-a



MOF-14A

Fig. 2. Two MOF-14 frameworks (blue and red) interwoven about a *P*-minimal surface without intersecting the surface.



Banglin Chen,1 M. Eddaoudi, S. T. Hyde,2 M. O' Keeffe, O. M. Yaghi, Science, 291, 1021-1023 (2001),

### Linking square and tetrahedron





MOF-11 Cu<sub>2</sub>(adamantane tetracarboxylate)

Notice that the Cu atoms in the paddle wheels are only 4-coordinated in the dehydrated form shown.

B. Chen, M. Eddaoudi, T. M. Reineke, J. W. Kampf, M. O' Keeffe, O. M. Yaghi J. Am. Chem. Soc. 122, 11559 (2000)



MOF-36 Cu<sub>2</sub>(methane tetracarboxyllate) another decorated PtS

J. Kim, B. Chen, T. M. Reineke, H. Li, D. B. Moler, M. O' Keeffe, O. M. Yaghi J. Am. Chem. Soc. 123, 8293 (2001) Linking square and trigonal prism H.-C. Zhou et a;. JACS 2014, 136, 3983

stp-a




See J. R. Long group. JACS, 2006, 128, 16874 Angew. Chem int ed. 2007, 46, 419





Essentially the same metal SBU but now octahedra

porphyin bases tetrazole square linker

UTSA-57 Banglin Chen group Inorg. Chem. 2015, 54, 200





scu-a



# linker in UiO-66 basic Zr terephthalate

K. P. Lillerud group.JACS, 130, 13850 (3008)



The underlying 12-c net of UiO-66 is **fcu** shown here in augmented form **fcu-a** = **ubt**. It is the B net un  $UB_{12}$  (hence the symbol. It is also a packing of archimedean polyhedra





The Zr<sub>6</sub> cluster with eight points of extension in MOF-545 at corners of a cube.



O. M. Yaghi group Inorg. Chem.51. 6443 (2012)

The linker in **MOF-545** – an Fe porphyrin tetracarboxylate. A second way of linking square and cube





The underlying (4,8)-c net in MOF-545 shown as csq-a

The same Zr<sub>6</sub> cluster but now only six points of extension forming a planar hexagon.



## H.-C. Zhou group JACS, 135,17105 (2013)

# The linker is a nickel porphyrin tetracarboxylate





The net is **she**, shown here as **she-a** 





The same Zr<sub>6</sub> group but now with octahedral arrangement of points of extension (large balls) The other ligands are formate. MOF-808 H. Furukawa et al. JACS, 136, 4369 (2014)



Net is edgetransitive **spn** shown here in augmented form



## MOF-808

## from paper



view down [110]

An isoreticular example – same Zr SBU but longer arms on the trtopic linker X. Zou, H. C. Zhou et al. Angew. Chem **2015**, *54*, 149





A fifferent Zr<sub>6</sub> SBU with 12 points of extensiom





H.-C Zhou et al. JACS 2014, 136, 17714

shp-a



Cd<sub>4</sub> cluster with eight points of extension Kimoon Kim group Angew. Chem. Int. Ed. 43, 971 (2004)





The net, as expected is **flu** (fluorite) shown here as **flu-a** 





The edge-transitive net **ttt** shown as **ttt-a** 



# $SiZn_8(-CO2)_{12}$

S. Y. Fang *et al.* Chem.Commun. 2002, 472.



The net of points of extension is 6-**snu** The net of linked SBUs is **pcu** – primitive cubic lattice net All the previous examples have been of edge-transitive nets

#### structures with the **cor** (corundum) topology



## $Re_6Se_8(CN)_6SBU$







trigonal-prismatic SBU

Shenqian Ma et al (H.-C. Zhou group) Inorg. Chem. 2007, 46, 3432

-> 93,6)-c net. There is no edge-transitive net for linking triangle with trigonal prism. Best is net **sit** that is edge 2-transitive.

First structure with this topology actually MOF-39 (Yaghi group JACS 2001, 123, 8239)



sit-a

sit-c-a

In every example to date **sit** nets are found to be interpenetrating pairs **sit** is polar (symmetry *Imm*2) and pairs of opposite polarity intergrow (*Imma*)

## A MOF with 3 SBUs – Eddaoudi group



#### A second description with a 24-c tertiary building unit (TBU)



# The (3,4)-c net **ntt-a**

transitivity 3,2



So we start a new chapter:

edge 2-transitive trinodal nets.

transitivity 3 2 r s


#### more of the same net. A cubic close packing of $(Cu_2)_{12}$ polyhedra



one more example of 3 vertices, two links, Matzger group



**agw-a** transitivity 3,2 Another MOF with three SBUs from the USF group Eddaoudi-Zaworotko Angew, Chem. Int. Ed. 52, 2902 (2013).





The net **asc-a** transitivity 3,2

#### MOF-505. Two ways of deconstructing



structure

as (3,4)-c net (**fof**) as

as 4-c net (nbo)

which way is best?

M. Li, D. Li, M. O'K. & O. M. Y., Chem. Rev. 114, 1343 2014)



#### as central link is lengthened, the structure gets far from cubic!

To retrieve fill topological information it is best to describe the (3,4)-c net derived from the 4-c net **nbo** 

The reason for this is that there can be many derived nets....

# There are two (3,4)-c nets derived from **nbo** with the same symmetry *R*-3*m* and transitivity 2,2



Both are observed in real MOFs

# **basic net** (4,*n*)-c, **derived net** (3,*n*)-c replace square or tetrahedral node



### (3,4)-c nets derived from **pts**



MTCNQ M = Cu, Ag -> **pts**-derived nets



basic net	transitivity	coord	replace	derived nets	transitivity
nbo	11	4	square	<sup>†</sup> fof, <sup>†</sup> fog, <sup>†</sup> tfb	22
lvt	11	4	square	<sup>†</sup> lil, <sup>†</sup> lim	22
rhr	11	4	square	ucp	22
cds	12	4	square	<sup>†</sup> gwg	23
dia	11	4	tetrahedron	tfa	22
qtz	11	4	tetrahedron	tfq	22
sod	11	4	tetrahedron	xbl	22
lon	12	4	tetrahedron	<sup>†</sup> zyl	34
pts	21	44	square	<sup>†</sup> dmd, <sup>†</sup> tfi	22
			square	<sup>†</sup> dmg, <sup>†</sup> dmh	3 3, 3 4
			tetrahedron	<sup>†</sup> sur, tfk	22
pth	21	44	square	hst	22
			tetrahedron	<sup>†</sup> phw, phx	22
ssb	21	44	square 1	<sup>†</sup> stu, stw	22
			square 2	stj, <sup>†</sup> stx	2 2
ssa	21	44	square 1	<sup>†</sup> sty	22
stp	21	64	square	ttp, ttx	2 2
soc	21	64	square	<sup>†</sup> edq, cdj	22
scu	21	84	square	tty	22
csq	21	84	square	<sup>†</sup> xly, xlz	22
ftw	21	12 4	square	ttv	22
iac	21	64	tetrahedron	<sup>†</sup> act	22
toc	21	64	tetrahedron	xab	22
cor	22	64	tetrahedron	<sup>†</sup> ttu	23

table from Li, M.; Li, D. O'Keeffe, M, Yaghi, O. m. Chem. Rev. b2014, 114, 1343

#### The strange story of Eddaoudi's queer structure



First a reminder of a common SBU with trigonal prismatic shape

linked by a
planar
tetratopic
linker ->
a cubic
structure!



(a)

Each SBU is linked to six others in an octahedral arrangement

The basic net is (4,6)-c **soc** for linking square and octahedron



### basic net linked square and octahedron



#### derived net



cdj-a

## look the octahedra have morphed into trigonal prisms!



edq-a

#### soc-a



These two nets have the same vertex symbol and coordination sequence. But you can see they are different. (Different symmetry!)

# hexatopic linker + octahedral SBU -> another net with three vertices and two edges



Banglin Chen group Cryst. Growth Des. 10, 2775 (2010)



#### net is **zxc**

<-



### net is **zxc**

<-

# structure of $CaCO_3 ! ->$



Planar hexatopic linker joined to paddlewheels -> (3,4)-c net not derived from a known (4,6)-c net

Net is **ntt** again and may authors use (3,24)-c description

edge 2-transitive trinodal nets.



We want to use the description with two kinds of link







J. T. Hupp group. *Cryst. Growth Des.* **2012**, *12*, 1075 JACS **2012**, *134*, 15046

#### But a twist... Now the linker isn't planar.



Banglin Chen group, Angew. Chem. 50, 3178 (2011)

But another net (**zyg**) with three vertices and two edges i.e. minimal transitivity 3 2

Suppose you are designing a MOF with a square metal SBU and a planar hexatopic linker. The edge-transitive net for linking square and hexagon is **she**. But surprise! - the square morphs into a tetrahedron.



she-a

het-a

### octatopic linkers





Example of an octatopic linker joining 3-c SBU's Wenbin Lin group



The (3,4)-c net **tfe** derived from the (3,8)-c net **the** 

Transitivity 3 2





blue Zn Green P red O black C

#### Zn<sub>16</sub>(HPO<sub>3</sub>)<sub>4</sub>(-CO<sub>2</sub>)<sub>24</sub>

Unprecedented 24-c SBU in IFMC-200. D. –Y. Du et al. Sci. Rep. 2013, 3, 2616



#### The linker in IFMC-200



#### The net **ddy** in augmented form **ddy-a**





augmented 3,4,24-c net ddy-a

augmented 4,12-c net **ftw-a**
Minimal transitivity. A minimal transitivity net has transitivity defined by the local arrangement of linkers and metal SBUs

Example of an exception MOF-177 has 6-c metal SBUs joined by tritopic linkers. Minimal transitivity is 2,1

Real material has net **qom** with transitivity 5,5



The local geometry uniquely determines the structure M. O'Keeffe. *Mat. Res. Bull.* **2006**, *41*, 911



# MOF-500 Yaghi group

### MIL-101 Férey group

*Angew. Chem* 2004, 43, 6295 Science, 2005, 309, 2040 Angew. Chem 2006, 46, 2528

The Férey unit and this one (below) have the **mtn** topology The Yaghi ubit had the **dia** topology. Why?





mtn-e

Hexamethylenetetramine linked by Cd atoms Shilun Qiu et al. (Jilin) *Angew. Chem. Int. Ed.* **2005**, 44, 3845.



staggered

eclipsed

### Linking staggered tetrahedra with $T-X-T = 180^{\circ}$ . Only one solution:



"cristobalite" *Fd*-3*m* two kinds of tetrahedra *F*-43*m* end of story for MOF-500 What about eclipsed tetrahedra and  $T-X-T = 180^{\circ}$ ?

No exact solution: D

### simple polyhedron with 5-sided fces



 $T-X-T = 177.1^{\circ}$  with regular tetrahedra OK we will take that, but...

The plot thickens.

If we pack dodecahedra so four meet at each vertex we get a finite structure in positively-curved space (a tiling of the 3-sphere = a 4-dimensional polytope).

To get a tiling of Euclidean 3-space we have to add in some polyhedra with six-sided faces.

So now we must ask what structures exist for simple tilings with 5- and six-sided faces?

Olaf Delgado to the rescue...

The dual problem is to find tilings by tetrahedra so that either five or six meet at an edge,

This has been done exhaustively for up to eleven kinds of tetrahedron.[ Delgado-Friedrichs, O.; O'Keeffe, M. *Acta cryst.* **2010**, *A66*, 637]

The two simplest have 3 kinds of tetrahedron and correspond to the well-known Frank-Kasper phases  $MgCu_2$  and  $Cr_3Si$ . The duals are also well known as the Type I and Type II clathrate structures. Their nets have symbols **mtn** and **mep**.

At this point one can simply show that one of the two proposed structures exactly fits the powder pattern.

This is basically what was done by the Férey group. But note they found the candidate structures by an entirely different procedure.

The answer was a structure based on **mtn** 

In fact we can show it is the preferred structure - closest to regular tetrahedra and  $T-X-T = 180^{\circ}$ .





mtn

mtn-e



but the SBUs are really trigonal prisms. net is mtn-e-a = mgc-x-d-e-a!





# SBU in Ti MOF from Férey group



# Be MOF from Jeff Long group











Some edge-transitive ways of linking ladders



MOF-75 points of extension of rod form twisted ladder. Net is **irl**. Yaghi Group JACS **2005**, *127*, 1504



Scandium terephthalate two groups, 2005



# net of scandium terephthalate

First view of the structure

Rods of AlO<sub>6</sub> octahedra

Norbert Stock group Inorg. Chem. 52, 1854 (2013)



One rod

large black balls are points of extension





# rods are not parallel



The binodal net **cua** 





two distinct tetragonal rod packings

rods are edge-shared tetrahedra

mss



pyrazole-based linker



rod points of extension are edge-sharing tetrahedra



Because we are taking points of extension as nodes of the net, it is in a sense alredy augmented. accordingly represent the 3-c ode a triangle

UTSA-30 Banglin Chen group. Net is **hyb** Chem. Commun, 49, 10856 (2012)

### MOFs with rod SBUs



MOF-74. One of the most promising materials for gas storage/separations

N. Rosi, J. Kim, M. Eddaoudi, B. Chen, M.O'Keeffe, O. M. Yaghi, JACS 2005, 127, 1504

50 Å 0000 Q 5000 不 7.0 A 业 HOLO HOLO to HOTO HOTO HO DOT, I VI IX XI П 10 IV ٧ VII

в

 ${M_3[(-O)_3(-CO_2)_3]}_{=}$  (M = Mg, Zn)





H. Deng, S. Grunder,
K. E. Cordova, C. Valente,
H. Furukawa, M. Hmadeh,
F. Gandara, A. C. Whalley,
Z. Liu, S. Asahina, H. Kazumori,
, M. O'Keeffe,O. Terasaki,
J. F. Stoddardt, O. M. Yaghi.
Science May 25, 2012.

"breathing" MOFs, especially rod MOFs G. Férey & C. Serre, *Chem. Soc. Rev.* 38, 380 (2009)

Special case of flexibility We can consider carboxylate link as a hinge Berend Smit *et al. JACS* 136. 2228 (2014)



The case of MOF-5 planar terephthalate groups non coplanar (and opposed) hinges - RIGID



The case of MOF-2355 terephthalate again 6-c acs net - hinges in parallel planes - FLEXIBLE


MOF-61, MOF-71, MIL-47, MIL-53 all have the **sra** net.

MIL-53 is the classical "breathing MOF"

rod MOFs. MOF-71 terephthalate again 4-c **sra** net - hinges in parallel planes - FLEXIBLE

## 3-periodic "SBU" Cd malonate



S. Yuan et al, Acta cryst. 2012 C68, m57 sod net

## Zeolitic Imidazolate Frameworks (ZIFs)



Park, K. S.; Ni, Z.; Côté, A. P.; Choi, J. Y.; Huang, R.; Uribe-Romo, F. J.; Chae, H. K.; O'Keeffe, M.; Yaghi, O. M. PNAS, 2006, 103, 10186. A. Phan, C. Doonan, F. J. Uribe-Romo, C. B. Knobler, M. O'Keeffe, O. M.Yaghi, Accts. Chem. Res. 43, 59 (2010)







ZIF-2 (crb) Zn $(\sqrt{N})_2$ 







ZIF-10 (mer) Zn $(\sqrt{N})_2$  Extensive set of functionalized imidazolate links e.g.:







ZIF-20 (Ita) Zn $(\overset{N}{\succ})_{2}$ 

N

O. M. Yaghi, et al. *Nature Materials* 2007, **6**, 501







ZIF-11 (rho) Zn $(\sum_{N \in \mathbb{Z}})_2$  O. M. Yaghi, et al. *Science* 2008, **319**, 939







ZIF-70 (gme) Zn $(N, \overline{}, N)$ N $(N, \overline{}, N)$ 

O. M. Yaghi, et al. *Science* 2008, **319**, 939







ZIF-69 (gme) Zn $(N \times V)$  ( $N \times V$ ) NO<sub>2</sub>



## Giant ZIFs - the cage in ZIF-100



M. O'Keeffe, O. M. Yaghi et al. Nature. 2008, 453, 207

end